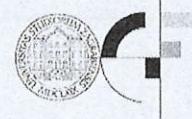


OPTPORNOST MATERIJALA 1

1. kolokvij, 15. studenoga 2021.

Grupa

B

Prezime i ime:

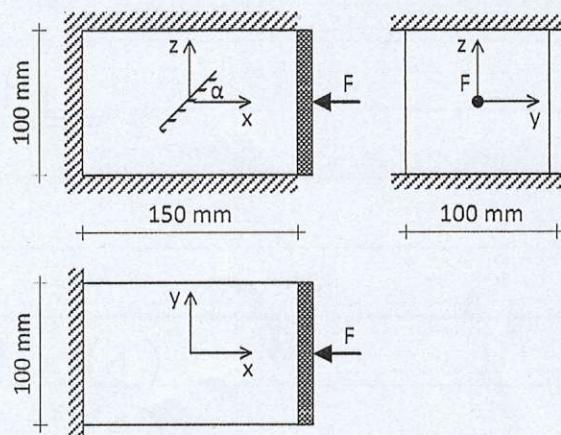
Čelična prizma opterećena je silom F prema slici.

Odredite:

- a) stanje naprezanja i deformacija u smjerovima x , y i z ,
- b) apsolutnu promjenu volumena prizme,
- c) puno naprezanje za ravninu koja sa osi x zatvara kut od $\alpha = 45^\circ$ (skica).

Zadano:

$$F = 500 \text{ kN}, E = 200 \text{ GPa}, \nu = 0,3$$



Za zadani štapni sustav odredite pomak točke D i naprezanja u štapovima 1 i 2 nakon spajanja štapa 1 s gredom.

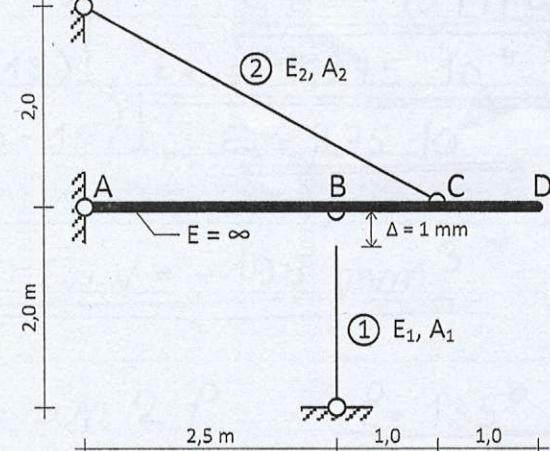
Zadano:

$$E_1 = 150 \text{ GPa}$$

$$E_2 = 210 \text{ GPa}$$

$$A_1 = 200 \text{ mm}^2$$

$$A_2 = 300 \text{ mm}^2$$



Na čeličnu cijev djeluju pritisak p_1 i promjena temperature ΔT . Odredite pritisak p_1 i pritisak p između čelične cijevi i aluminijskog valjka ako je uslijed opisanih djelovanja na cijev došlo do smanjenja promjera valjka za $\Delta D = 0,02 \text{ mm}$.

Zadano:

$$E_{\text{čelik}} = 200 \text{ GPa}$$

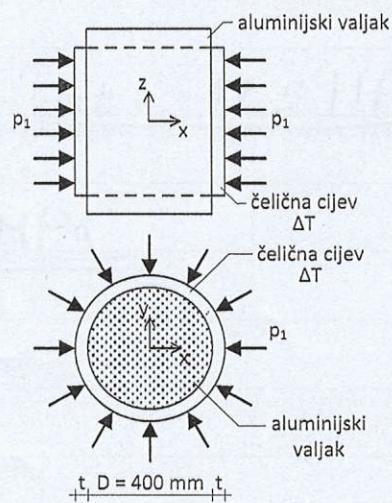
$$E_{\text{aluminij}} = 80 \text{ GPa}$$

$$\nu_{\text{aluminij}} = 0,35$$

$$\alpha_t, \text{čelik} = 1,25 \cdot 10^{-5} \text{ 1/K}$$

$$t = 6 \text{ mm}$$

$$\Delta T = -30 \text{ K}$$



$$F = 500 \text{ kN}$$

$$E = 200 \text{ GPa}$$

$$\nu = 0,3$$

$$\tilde{\sigma}_x = -\frac{F}{A} = \frac{-500 \cdot 10^3}{100^2} = -50 \text{ MPa}$$

$$\tilde{\sigma}_y = 0, \quad \tilde{\sigma}_z \neq 0$$

$$\varepsilon_x = \frac{1}{E} [\tilde{\sigma}_x - \nu (\tilde{\sigma}_y + \tilde{\sigma}_z)] \neq 0 \quad (1)$$

$$\varepsilon_y = \frac{1}{E} [\tilde{\sigma}_y - \nu (\tilde{\sigma}_x + \tilde{\sigma}_z)] \neq 0 \quad (2)$$

$$\varepsilon_z = \frac{1}{E} [\tilde{\sigma}_z - \nu (\tilde{\sigma}_x + \tilde{\sigma}_y)] = 0 \quad (3) \rightarrow \tilde{\sigma}_z = \nu \tilde{\sigma}_x$$

$$\tilde{\sigma}_z = -15 \text{ MPa}$$

$$\rightarrow \text{iz (1)} \Rightarrow \varepsilon_x = \frac{1}{2 \cdot 10^5} [-50 - 0,3 \cdot (-15)], \quad \varepsilon_x = -2,275 \cdot 10^{-4}$$

$$\rightarrow \text{iz (2)} \Rightarrow \varepsilon_y = \frac{1}{2 \cdot 10^5} [-0,3 \cdot (-50 - 15)], \quad \varepsilon_y = 9,75 \cdot 10^{-5}$$

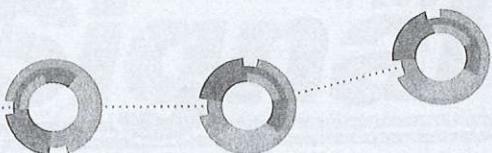
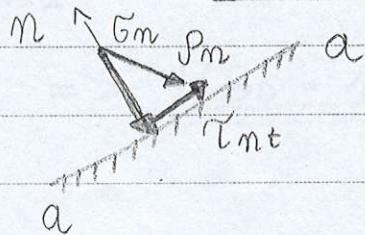
$$\varepsilon_v = \varepsilon_x + \varepsilon_y + \varepsilon_z = -1,3 \cdot 10^{-4}, \quad \Delta V = \varepsilon_v \cdot V = -195 \text{ mm}^3$$

$$\tilde{\sigma}_n = \tilde{\sigma}_x \cos^2 \rho + \tilde{\sigma}_z \sin^2 \rho + \tau_{xz} \sin 2 \rho \quad \rho = 135^\circ$$

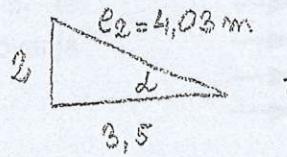
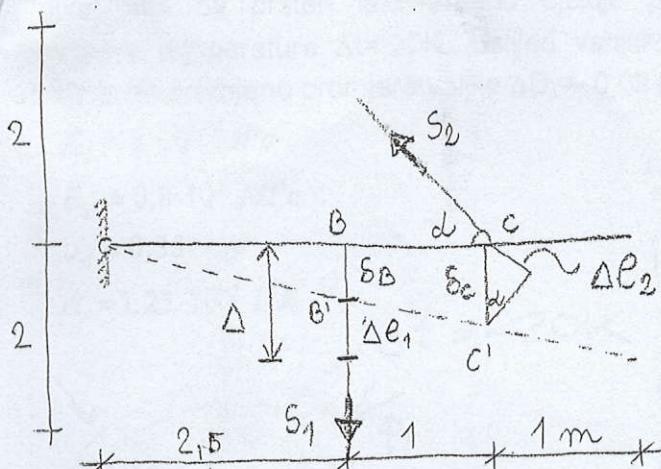
$$\tilde{\sigma}_n = -32,5 \text{ MPa} \quad \tau_{xz} = 0$$

$$\tau_{nt} = \frac{\tilde{\sigma}_z - \tilde{\sigma}_x}{2} \sin 2 \rho + \tau_{xz} \cos 2 \rho, \quad \tau_{nt} = -17,5 \text{ MPa}$$

$$\sigma_n = \sqrt{\tilde{\sigma}_n^2 + \tau_{nt}^2}, \quad \sigma_n = 36,91 \text{ MPa}$$



2. ZADATAK



$$\operatorname{tg} \alpha = \frac{d}{3,5}$$

U.R. : $\alpha = 29,74^\circ$

$$S_1 \cdot 2,5 = S_2 \sin \alpha \cdot 3,5$$

$$S_1 = 0,695 S_2; S_2 = 1,44 S_1$$

V.D.

$$\frac{\delta_c}{3,5} = \frac{\delta_B}{2,5}$$

$$\delta_c = \frac{\Delta \epsilon_2}{\sin \alpha} = \frac{S_2 \cdot \epsilon_2}{E_2 A_2 \sin \alpha}$$

$$\delta_c = \delta_B \cdot 1,4$$

$$\delta_B = \Delta - \Delta \epsilon_1 = \Delta - \frac{S_1 \cdot \epsilon_1}{E_1 \cdot A_1}$$

$$\frac{S_2 \cdot \epsilon_2}{E_2 \cdot A_2 \cdot \sin \alpha} = \left(\Delta - \frac{S_1 \cdot 0,694 \cdot \epsilon_1}{E_1 \cdot A_1} \right) \cdot 1,4$$

| $S_2 = 7,22 \text{ kN}$

| $S_1 = 5,01 \text{ kN}$

| $G_1 = 25,07 \text{ MPa}$

| $G_2 = 24,08 \text{ MPa}$

$$\Delta \epsilon_2 = \frac{S_2 \cdot \epsilon_2}{E_2 \cdot A_2} \cdot 0,46 \text{ mm} \Rightarrow \delta_c = 0,93 \text{ mm}$$

$$\frac{\delta_D}{4,5} = \frac{\delta_c}{3,5} \Rightarrow | \delta_D = 1,2 \text{ mm}$$

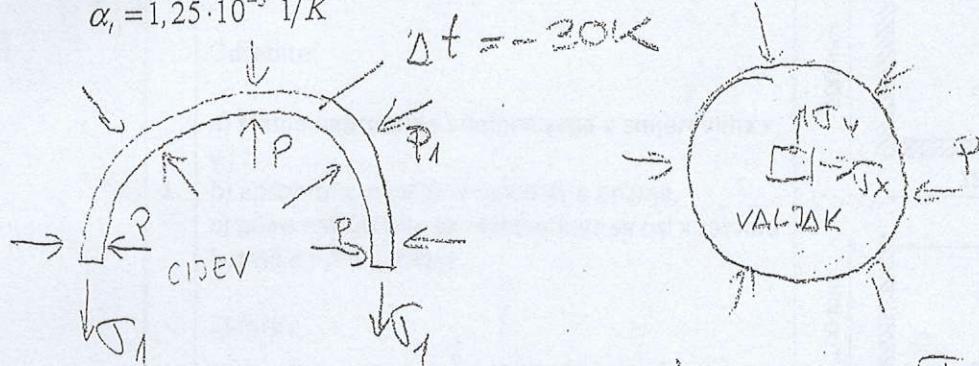
otrebno je odrediti međusobni pritisak p između prstena i valjka, ako na prsten istovremeno djeluje pritisak p_1 te promjena temperature $\Delta t = -30K$. Uslijed vanjskog djelovanja došlo je do promjene promjera valjka $\Delta D_1 = -0,02 \text{ mm}$.

$$E_c = 2 \cdot 10^5 \text{ MPa}$$

$$E_{al} = 0,8 \cdot 10^5 \text{ MPa}$$

$$\nu_{al} = 0,35$$

$$\alpha_c = 1,25 \cdot 10^{-5} \text{ 1/K}$$



$$\cancel{\sigma_1 \cdot t \cdot b + P_1(D+2t)b = PD \cdot b}$$

$$\boxed{\sigma_1 = \frac{PD - P_1(D+2t)}{2t}}$$

$$\begin{aligned} \sigma_x &= \sigma_y = -P \\ \sigma_z &= 0 \end{aligned}$$

$$\epsilon_c = \epsilon_{al} = \frac{\Delta D}{D} = \frac{-0,02}{400} = -5 \cdot 10^{-5}$$

$$\epsilon_{al} = \frac{1}{E_{al}} (\sigma_x - \nu (\sigma_y + \sigma_z)) = -5 \cdot 10^{-5}$$

$$-P + \nu P = -4 \Rightarrow \boxed{P = 6,15 \text{ MPa}}$$

$$\epsilon_{c,al} = \frac{\sigma_x}{E_c} + \nu t \cdot \Delta t = -5 \cdot 10^{-5}$$

$$\frac{PD - P_1(D+2t)}{2t \cdot E_c} + \nu t \cdot \Delta t = -5 \cdot 10^{-5}$$

$$1,025 \cdot 10^{-3} - 17,14 \cdot 10^{-5} \cdot P_1 = -5 \cdot 10^{-5} + 37,5 \cdot 10^{-5}$$

$$\boxed{P_1 = 4,08 \text{ MPa}}$$

